

Package ‘coRanking’

July 22, 2025

Title Co-Ranking Matrix

Version 0.2.5

Description Calculates the co-ranking matrix to assess the quality of a dimensionality reduction.

URL <https://coranking.guido-kraemer.com/>

BugReports <https://github.com/gdkrmr/coRanking/issues>

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Encoding UTF-8

Imports methods, graphics, stats

RoxygenNote 7.3.2

Collate 'coranking-package.R' 'coranking.R' 'coranking_internals.R' 'lcmc.R' 'criteria.R' 'image.R' 'rankmatrix.R' 'submatrix.R' 'r_nx.R'

Suggests testthat, knitr, rmarkdown, Rtsne, scatterplot3d

VignetteBuilder knitr

NeedsCompilation yes

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Repository CRAN

Date/Publication 2024-09-30 09:30:02 UTC

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coRanking-package	<i>Methods for the co-ranking matrix</i>
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Description

coRanking provides methods for the calculation of the co-ranking matrix and derived measures to assess the quality of a dimensionality reduction

Details

This package provides functions for calculating the co-ranking matrix, plotting functions and some derived measures for quality assessment of dimensionality reductions.

Funding provided by the Department for Biogeochemical Integration, Empirical Inference of the Earth System Group, at the Max Plack Institute for Biogeochemistry, Jena.

Author(s)

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References

- Chen, L., Buja, A., 2006. Local Multidimensional Scaling for Nonlinear Dimension Reduction, Graph Layout and Proximity Analysis.
- Lee, J.A., Lee, J.A., Verleysen, M., 2009. Quality assessment of dimensionality reduction: Rank-based criteria. *Neurocomputing* 72.
- Lueks, W., Mokbel, B., Biehl, M., & Hammer, B. (2011). How to Evaluate Dimensionality Reduction? - Improving the Co-ranking Matrix. *ArXiv:1110.3917 [Cs]*. <http://arxiv.org/abs/1110.3917>
- Lee, J. A., Peluffo-Ordóñez, D. H., & Verleysen, M., 2015. Multi-scale similarities in stochastic neighbour embedding: Reducing dimensionality while preserving both local and global structure. *Neurocomputing*, 169, 246–261. <https://doi.org/10.1016/j.neucom.2014.12.095>

See Also

Useful links:

- <https://coranking.guido-kraemer.com/>
- Report bugs at <https://github.com/gdkrmr/coRanking/issues>

AUC_{ln}K*Area under the R_{NX} curve***Description**

Area under the $R_{NX}(K)$ curve when K is put on a logarithmic scale.

Usage

AUC_{ln}K(R_{NX})

Arguments

R_{NX} The R_{NX} curve, a vector of values

Details

It is calculated as:

$$AUC_{\ln K}(R_{NX}(K)) = \left(\sum_{K=1}^{N-2} R_{NX}(K)/K \right) / \left(\sum_{K=1}^{N-2} 1/K \right)$$

Value

A value, the area under the curve.

Author(s)

Guido Kraemer

References

Lee, J. A., Peluffo-Ordóñez, D. H., & Verleysen, M., 2015. Multi-scale similarities in stochastic neighbour embedding: Reducing dimensionality while preserving both local and global structure. *Neurocomputing*, 169, 246–261. <https://doi.org/10.1016/j.neucom.2014.12.095>

`coranking`*Co-Ranking Matrix*

Description

Calculate the co-ranking matrix to assess the quality of a dimensionality reduction.

Usage

```
coranking(  
  Xi,  
  X,  
  input_Xi = c("data", "dist", "rank"),  
  input_X = input_Xi,  
  use = "C"  
)
```

Arguments

<code>Xi</code>	high dimensional data
<code>X</code>	low dimensional data
<code>input_Xi</code>	type of input of Xi (see. details)
<code>input_X</code>	type of input of X (see. details)
<code>use</code>	R or C backend

Details

Calculate the coranking matrix, to assess the quality of a dimensionality reduction. `Xi` is input in high dimensions, `X` is input in low dimensions the type of input is given in `input_Xi` and `input_X`, they can be one of `c('data', 'dist', 'rank')`.

Value

a matrix of class `'coranking'`

Author(s)

Guido Kraemer

See Also

[rankmatrix](#)

`imageplot`*Image function for the co-ranking matrix*

Description

Plots the co-ranking matrix nicely

Usage

```
imageplot(  
  Q,  
  lwd = 2,  
  bty = "n",  
  main = "co-ranking matrix",  
  xlab = expression(R),  
  ylab = expression(Ro),  
  col = colorRampPalette(colors = c("gray85", "red", "yellow", "green", "blue"))(100),  
  axes = FALSE,  
  legend = TRUE,  
  ...  
)
```

Arguments

<code>Q</code>	of class <code>coranking</code> .
<code>lwd</code>	linewidth in legend
<code>bty</code>	boxtype of legend
<code>main</code>	title of plot
<code>xlab</code>	label of the x axis
<code>ylab</code>	label of the y axis
<code>col</code>	a palette for coloring
<code>axes</code>	logical draw axes
<code>legend</code>	if T plot a legend.
<code>...</code>	parameters for the <code>image</code> function.

Details

Plots the co-ranking matrix nicely for visual inspection. uses the `image` function internally, `...` is passed down to the `image` function. The values in the co-ranking matrix are logscaled for better contrast.

Author(s)

Guido Kramer

 LCMC

The local continuity meta-criterion

Description

Calculate the local continuity meta-criterion from a co-ranking matrix.

Usage

```
LCMC(Q, K = 1:nrow(Q))
```

Arguments

Q a co-ranking matrix
 K vector of integers describing neighborhood size

Details

The local continuity meta-criterion (Chen and Buja, 2006) is defined as

$$LCMC = \frac{K}{1-N} + \frac{1}{NK} \sum_{(k,l) \in UL_K} q_{kl}$$

Higher values mean a better performance of the dimensionality reduction.

Value

A number, the local continuity meta-criterion

Author(s)

Guido Kraemer

 plot_R_NX

Plot the R_NX(K) curve

Description

Produces a plot with the $R_{NX}(K)$ curves from the arguments

Usage

```
plot_R_NX(R_NXs, pal = grDevices::palette(), ylim = c(0, 0.9), ...)
```

Arguments

R_NXs	A list of R_NX curves, names from the list will appear in the legend
pal	a vector of colors
ylim	set the y-axis limits of the plot
...	options for the plotting function

Value

Nothing, produces a plot.

Author(s)

Guido Kraemer

References

Lee, J. A., Peluffo-Ordóñez, D. H., & Verleysen, M., 2015. Multi-scale similarities in stochastic neighbour embedding: Reducing dimensionality while preserving both local and global structure. *Neurocomputing*, 169, 246–261. <https://doi.org/10.1016/j.neucom.2014.12.095>

Q_NX

The $Q_{NX}(K)$ criterion

Description

A curve indicating the percentage of points that are mild in- and extrusions or keep their rank.

Usage

Q_NX(Q)

Arguments

Q a co-ranking matrix

Details

$$Q_{NX}(K) = \frac{1}{KN} \sum_{k=1}^K \sum_{l=1}^K Q_{kl}$$

Value

A vector with the values for Q_NX(K)

Author(s)

Guido Kraemer

References

Lueks, W., Mokbel, B., Biehl, M., & Hammer, B. (2011). How to Evaluate Dimensionality Reduction? - Improving the Co-ranking Matrix. ArXiv:1110.3917 [Cs]. <http://arxiv.org/abs/1110.3917>

rankmatrix

Rank matrix

Description

Replaces the elements of X with their rank in the column vector of the distance matrix

Usage

```
rankmatrix(X, input = c("data", "dist"), use = "C")
```

Arguments

<code>X</code>	data, dist object, or distance matrix
<code>input</code>	type of input
<code>use</code>	if 'C' uses the compiled library, else uses the native R code

Details

Each column vector in the distance matrix (or the distance matrix computed from the input) is replaced by a vector indicating the rank of the distance inside that vector.

This is a computation step necessary for the co-ranking matrix and provided mainly so that the user has the possibility to save computation time.

Value

returns a matrix of class 'rankmatrix'

Author(s)

Guido Kraemer

R_NX

*The R_NX(K) criterion***Description**

A curve indicating the improvement of the embedding over a random embedding for the neighborhood size K . Values range from 0, for a random embedding, to 1 for a perfect embedding.

Usage

R_NX(Q)

Arguments

Q a co-ranking matrix

Details

$R_{NX}(K)$ is calculated as follows:

$$Q_{NX}(K) = \sum_{1 \leq k \leq K} \sum_{1 \leq l \leq K} \frac{q_{kl}}{KN}$$

Counts the upper left K -by- K block of Q , i.e. it considers the preserved ranks on the diagonal and the permutations within a neighborhood.

$$R_{NX}(K) = \frac{(N-1)Q_{NX}(K) - K}{N-1-K}$$

A resulting value of 0 corresponds to a random embedding, a value of 1 to a perfect embedding of the K -ary neighborhood.

Value

A vector with the values for R_NX(K)

Author(s)

Guido Kraemer

References

Lee, J.A., Lee, J.A., Verleysen, M., 2009. Quality assessment of dimensionality reduction: Rank-based criteria. *Neurocomputing* 72.

Lee, J. A., Peluffo-Ordóñez, D. H., & Verleysen, M., 2015. Multi-scale similarities in stochastic neighbour embedding: Reducing dimensionality while preserving both local and global structure. *Neurocomputing*, 169, 246–261. <https://doi.org/10.1016/j.neucom.2014.12.095>

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